

# Physics Formula Sheet

## Unit Conversions

Length: 1 meter = 39.37 inches = 3.281 feet, 1 km = 0.621 miles, 1 mile = 5280 feet = 1609 meters

Mass: 1 amu (u) =  $1.66 \times 10^{-27}$  kg      Mass-Energy: (1 u) \* 931.5 = Energy (MeV)

Time: 1 hour = 3600 seconds, 1 year = 365.25 days =  $3.16 \times 10^7$  sec

Volume: 1 Liter = 1000 cm<sup>3</sup> =  $10^{-3}$  m<sup>3</sup>, 1 gallon = 3.786 L =  $3.786 \times 10^{-3}$  m<sup>3</sup> = 231 in<sup>3</sup>

Force: 1 Newton = 1 kg·m/s<sup>2</sup> = 0.2248 pounds      Angular Measure: 1 rev = 360° =  $2\pi$  rad

Energy: 1 Joule = 0.239 cal = 0.738 ft·lb, 1 kw·hr =  $3.6 \times 10^6$  J, 1 eV =  $1.60 \times 10^{-19}$  J

Pressure: 1 atm =  $1.013 \times 10^5$  Pascals (N/m<sup>2</sup>) = 29.92 inches or 760 mm of Hg

Temperature:  $T_F = 1.8 \cdot T_C + 32$ ,  $T_C = 0.556 \cdot (T_F - 32)$ ,  $T_K = T_C + 273$

Density: 1 g/cm<sup>3</sup> = 1000 kg/m<sup>3</sup>

Radioactivity: 1 Bq =  $2.7 \times 10^{-11}$  Ci

## Physical Constants

Mass of Earth:  $M_E = 5.98 \times 10^{24}$  kg

Radius of Earth:  $R_E = 6.38 \times 10^6$  m

Mass of Sun:  $M_S = 1.99 \times 10^{30}$  kg

Earth-Sun distance:  $r_E = 1.5 \times 10^{11}$  m

Gravitational Constant:  $G = 6.67 \times 10^{-11}$  N·m<sup>2</sup>/kg<sup>2</sup>

Speed of Light:  $c = 3.0 \times 10^8$  m/s

Electron mass:  $m_e = 0.0005486$  u =  $9.11 \times 10^{-31}$  kg

Proton mass:  $m_p = 1.007276$  u =  $1.67 \times 10^{-27}$  kg

Neutron mass:  $m_n = 1.008665$  u =  $1.67 \times 10^{-27}$  kg

Helium mass:  $m_{He} = 4.002602$  u =  $6.64 \times 10^{-27}$  kg

Boltzmann's Constant:  $k_B = 1.38 \times 10^{-23}$  J/K

Avogadro's #:  $N_A = 6.023 \times 10^{23}$  molecules/mole

Ideal Gas Constant:  $R = 8.31$  J/mol·K = 0.0821 L·atm/mol·K

Stefan-Boltzmann Radiation Constant:  $\sigma = 5.67 \times 10^{-8}$  W/m<sup>2</sup>·K<sup>4</sup>

Specific heat of water:  $c_{\text{water}} = 4186$  J/kg·°C

Latent heat of fusion:  $L_f = 333,000$  J/kg

Specific heat of ice:  $c_{\text{ice}} = 2090$  J/kg·°C

Latent heat of vaporization:  $L_v = 2.26 \times 10^6$  J/kg

Specific heat of steam:  $c_{\text{steam}} = 2010$  J/kg·°C

Coulomb constant:  $k_c = 8.99 \times 10^9$  N·m<sup>2</sup>/C<sup>2</sup>

Permittivity of free space:  $\epsilon_0 = 8.85 \times 10^{-12}$  C<sup>2</sup>/N·m<sup>2</sup>

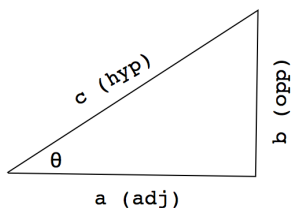
Fundamental charge:  $e = 1.60 \times 10^{-19}$  C

Permeability of free space:  $\mu_0 = 1.26 \times 10^{-6}$  T·m/A

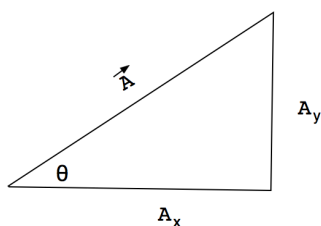
Planck's constant:  $h = 6.626 \times 10^{-34}$  J·s

Rydberg constant:  $R_H = 1.097 \times 10^7$  m<sup>-1</sup>

## Basic Trigonometry



$$\begin{aligned} a^2 + b^2 &= c^2 \\ \cos \theta &= \text{adj/hyp} \\ \sin \theta &= \text{opp/hyp} \\ \tan \theta &= \text{opp/adj} \\ \theta &= \tan^{-1}(\text{opp/adj}) \end{aligned}$$



$$\begin{aligned} A_x &= A \cos \theta \\ A_y &= A \sin \theta \\ \theta &= \tan^{-1}(|A_y|/|A_x|) \end{aligned}$$

## Motion with Constant Acceleration

Average velocity:  $v_{\text{avg}} = \Delta x / \Delta t$

Multi-part motion:  $\Delta x_1 = v_{\text{avg},1} t_1$ ,  $\Delta x_2 = v_{\text{avg},2} t_2$ , ...

$$\Delta x_{\text{tot}} = \Delta x_1 + \Delta x_2 + \dots = v_{\text{avg,tot}} t_{\text{tot}}$$

Acceleration:  $a = \Delta v / \Delta t = (v - v_0) / t$

If  $a = \text{constant}$ , then  $v_{\text{avg}} = (v + v_0) / 2$

where  $\Delta x = \text{displacement}$ ,

$v = \text{final velocity}$

$v_0 = \text{initial velocity}$

Equation of Motion

(1)  $\Delta x = \frac{1}{2}(v + v_0)t$

(2)  $v = v_0 + at$

(3)  $\Delta x = v_0 t + \frac{1}{2}at^2$

(4)  $\Delta x = vt - \frac{1}{2}at^2$

(5)  $v^2 = v_0^2 + 2a\Delta x$

Missing

**a**

**$\Delta x$**

**v**

**$v_0$**

**t**

## Forces (Newtons)

$$\sum \mathbf{F} = m\mathbf{a} \implies \sum \mathbf{F}_x = m\mathbf{a}_x, \sum \mathbf{F}_y = m\mathbf{a}_y \text{ or } \sum \mathbf{F}_{\parallel} = m\mathbf{a}_{\parallel}, \sum \mathbf{F}_{\perp} = m\mathbf{a}_{\perp}$$

### Force Definitions (Magnitude and Direction)

Gravity:  $\mathbf{F}_g = |mg|$ , downward, where  $g = 9.8 \text{ m/s}^2$

Applied:  $\mathbf{F}_{\text{App}} = |\text{variable}|$ ,  $|\text{variable}|$  (must be defined in problem statement or solved for)

Tension:  $\mathbf{F}_T = |\text{variable}|$ , inward from each end of rope/string, equal and opposite at each end

Normal:  $\mathbf{F}_N = |\sum \mathbf{F}_{\perp}|$  (sum of all other  $\perp$  forces),  $\perp$  to and out of surface.

Kinetic Friction:  $\mathbf{F}_{\text{KF}} = |\mu_k \mathbf{F}_N|$ , opposing motion, where  $\mu_k$  is the coefficient of kinetic friction.

Static Friction:  $\mathbf{F}_{\text{SF}} = |\sum \mathbf{F}_{\parallel}|$  (sum of all other  $\parallel$  forces), opposite direction of  $\sum \mathbf{F}_{\parallel}$ .

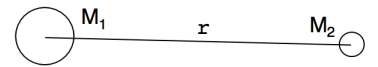
Static Friction (max value):  $\mathbf{F}_{\text{SF,max}} = |\mu_s \mathbf{F}_N|$  where  $\mu_s$  is the coefficient of static friction.

Spring:  $\mathbf{F}_{\text{spr}} = |k_s \Delta \mathbf{x}|$ , restoring,  $k_s =$  spring constant (N/m) and  $\Delta \mathbf{x} =$  displacement from equilibrium

"Centrifugal":  $\mathbf{F}_{\text{cf}} = |m\mathbf{v}^2/r|$  or  $|m\mathbf{r}\omega^2|$ , radially outward, where  $r =$  radius of circular motion

Buoyancy:  $\mathbf{F}_b = |\rho_f V_f g|$ , upward.  $\rho_f =$  fluid density,  $V_f =$  volume of displaced fluid

Newtonian Gravity:  $F_{\text{grav}} = \left| \frac{GM_1 M_2}{r^2} \right|$ , attractive



where  $G = 6.67 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2$ ,

$r =$  distance between centers of  $M_1$  and  $M_2$ .

Electric:  $F_{\text{electric}} = \left| \frac{k_c q_1 q_2}{r^2} \right|$ , like charges repel, opposites attract.

where  $k_c =$  Coulomb constant ( $8.99 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$ ),

$r =$  distance between centers of charges  $q_1$  and  $q_2$

More generally,  $F_{\text{Electric}} = qE$ , where  $E =$  Electric field in which  $q$  is immersed

Magnetic:  $\mathbf{F}_b = q\mathbf{v} \times \mathbf{B}$  or  $|q\mathbf{v}\mathbf{B}\sin\theta|$  for moving charges,

or  $l\mathbf{I} \times \mathbf{B}$  or  $l|\mathbf{I}\mathbf{B}\sin\theta|$  for current-carrying wires ( $l =$  length of wire),

direction: right-hand rule #1 ( $\mathbf{F} =$  palm,  $\mathbf{v}$  or  $\mathbf{I} =$  thumb,  $\mathbf{B} =$  fingers)

where  $\theta$  is the angle between  $\mathbf{v}$  and  $\mathbf{B}$  or between  $\mathbf{I}$  and  $\mathbf{B}$ . (cross product)

## Energy and Work (Joules)

### Work done by a Force

Work/Energy Units: 1 Joule =  $1 \text{ kg}\cdot\text{m}^2/\text{s}^2$ , 1 Watt = 1 Joule/sec

Method #1:  $W_F = |\mathbf{F}| \cdot |\Delta \mathbf{s}| \cdot \cos\theta$ , where  $\theta$  is the angle between  $\mathbf{F}$  and  $\Delta \mathbf{s}$

Method #2:  $W_F = -\Delta U_F$  or  $U_{\text{initial}} - U_{\text{final}}$ , where  $U_F$  is the potential energy related to the force

Method #3:  $W_{F1} + W_{F2} + W_{F3} = W_{\text{tot}}$ . Find  $W_{F1}$ ,  $W_{F2}$  and  $W_{\text{tot}}$ , then solve for  $W_{F3}$ .

### Potential Energy (only conservative forces have an associated potential energy)

Gravity (relative):  $\Delta U_{\text{grav}} = mg\Delta y$  (only works for small distances over which  $g = 9.8 \text{ m/s}^2$ )

Newtonian Gravity (absolute):  $U_{\text{grav}} = -\frac{GM_1 M_2}{r}$  (see diagram above)

Spring:  $U_{\text{spr}} = \frac{1}{2}k_s(\Delta \mathbf{x})^2$ , where  $k_s =$  spring constant (N/m),  $\Delta \mathbf{x} =$  displacement from equilibrium

Electric (relative):  $\Delta U_{\text{electric}} = q_1 \Delta V_2$ , where  $q_1$  is a charge immersed in a potential  $V_2$ .

Electric (absolute):  $U_{\text{electric}} = \frac{k_c q_1 q_2}{r}$ , where  $r =$  distance between centers of charges  $q_1$  and  $q_2$

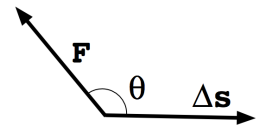
Work-Energy and Energy Conservation:  $U =$  potential energy,  $K = \frac{1}{2}mv^2$ , kinetic energy

Mechanical Energy:  $E = K + U$ .  $E$  is conserved ( $\Delta E = 0$ ) if only conservative forces do work

Work-Energy Theorem:  $W_{\text{tot}} = \sum W_F = \Delta K$ .

### Power (Watts) and Energy

Power:  $P = \text{Energy}/\text{time}$  or  $\text{Work}/\text{time}$ ,  $P = |\mathbf{F}| \cdot |\mathbf{v}| \cdot \cos\theta$ , where  $\theta$  is the angle between  $\mathbf{F}$  and  $\mathbf{v}$



## Momentum (kg·m/s) and Collisions

**Momentum:**  $\mathbf{p} = m\mathbf{v}$ , where  $\mathbf{p}$  = momentum (kg·m/s),  $\mathbf{p}$  and  $\mathbf{v}$  share the same direction.

**Impulse:**  $\Delta\mathbf{p} = \mathbf{F}_{\text{avg}}\Delta t$  or  $\mathbf{F}_{\text{avg}} = \Delta\mathbf{p}/\Delta t$ , where  $\Delta\mathbf{p} = \mathbf{p}_{\text{final}} - \mathbf{p}_{\text{initial}}$ .

**Momentum Conservation:** If  $\sum \mathbf{F}_{\text{ext}} = 0$ , then  $\Delta\mathbf{p} = 0$ , where  $\sum \mathbf{F}_{\text{ext}}$  = sum of all external forces.

If  $\Delta\mathbf{p} = 0$ , then:  $\Delta\mathbf{p}_x = 0$  or  $m_1\mathbf{v}_{1i,x} + m_2\mathbf{v}_{2i,x} = m_1\mathbf{v}_{1f,x} + m_2\mathbf{v}_{2f,x}$   
and  $\Delta\mathbf{p}_y = 0$  or  $m_1\mathbf{v}_{1i,y} + m_2\mathbf{v}_{2i,y} = m_1\mathbf{v}_{1f,y} + m_2\mathbf{v}_{2f,y}$

If masses stick together after collision, then  $\mathbf{v}_{1f} = \mathbf{v}_{2f} = \mathbf{v}_f$

**Elastic Collisions:** If  $\Delta\mathbf{p} = 0$  and  $\Delta K = 0$ , then:

$$v_{1f} = \frac{m_1 - m_2}{m_1 + m_2} v_{1i} + \frac{2m_2}{m_1 + m_2} v_{2i} \quad \text{and} \quad v_{2f} = \frac{2m_1}{m_1 + m_2} v_{1i} + \frac{m_2 - m_1}{m_1 + m_2} v_{2i}$$

**Shortcut:** Note that if  $m_1 = m_2$ , then  $v_{1f} = v_{2i}$  and  $v_{2f} = v_{1i}$ .

## Rotational Motion and Newtonian Gravity

**Angular equivalents:**  $\Delta\theta = \Delta s/r$ ,  $\omega = v/r$ ,  $\alpha = a_{\text{tan}}/r$

**Centripetal acceleration:**  $\mathbf{a}_{\text{cp}} = v^2/r$  or  $r\omega^2$ , directed radially inward

**"Centrifugal force":**  $\mathbf{F}_{\text{cf}} = mv^2/r$  or  $mr\omega^2$ , directed radially outward

### Motion with Constant $\alpha$

$$\Delta\theta = \frac{1}{2}(\omega + \omega_0)t$$

$$\omega = \omega_0 + \alpha t$$

$$\Delta\theta = \omega_0 t + \frac{1}{2}\alpha t^2$$

$$\Delta\theta = \omega t - \frac{1}{2}\alpha t^2$$

$$\omega^2 = \omega_0^2 + 2\alpha\Delta\theta$$

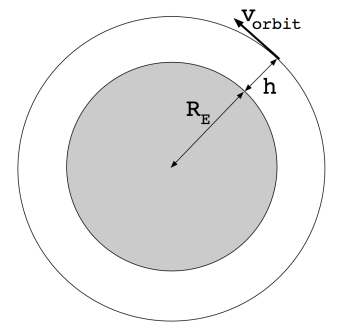
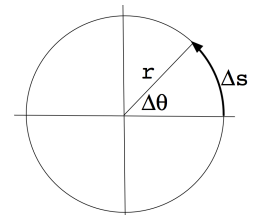
### Orbital Motion (Earth)

$r_{\text{orbit}} = R_E + h$ , where  $R_E$  = Radius of Earth,  
and  $h$  = altitude above surface

$2\pi r_{\text{orbit}} = v_{\text{orbit}}T$ , where  $T$  = orbital period

**Equation of Orbital Velocity:**  $v_{\text{orbit}} = \sqrt{\frac{GM}{r_{\text{orbit}}}}$

**Kepler's 3rd Law of Orbits:**  $T^2 = \left(\frac{4\pi^2}{GM}\right)r_{\text{orbit}}^3$



## Torque (Newton-meters)

**Torque (Cross Product):**  $\tau = \mathbf{r} \times \mathbf{F}$  or  $|\mathbf{r}| \cdot |\mathbf{F}| \cdot \sin\theta$ , where

$\mathbf{r}$  = distance vector from pivot to point of application of the force, and

$\theta$  = angle between tails of vectors  $\mathbf{r}$  and  $\mathbf{F}$ .

**Torque (Lever Arm):**  $\tau = |\mathbf{F}\ell|$ , where

$\ell$  =  $\perp$  distance to line of action or "lever arm".

**Sign Convention:**  $\tau$  is negative if directed clockwise (cw)

$\tau$  is positive if directed counter-clockwise (ccw).

**Moment of Inertia:**  $I = AMR^2$  (kg·m<sup>2</sup>), where

$R$  = radius of object and  $A$  = number from 0-1

depending upon the nature of the object

$$I_{\text{ring}} = MR^2$$

$$I_{\text{point mass}} = Mr^2, \text{ where } r = \text{distance from object to axis}$$

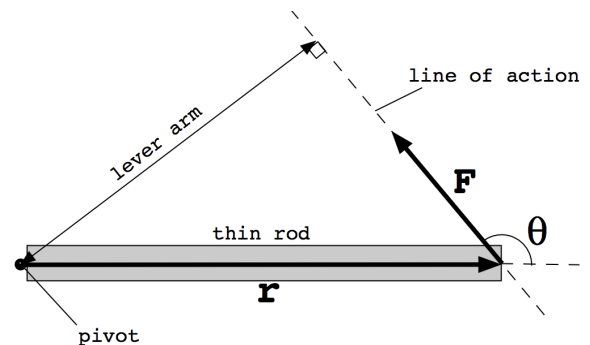
$$I_{\text{cylinder}} = \frac{1}{2}MR^2$$

$$I_{\text{sphere}} = 0.4MR^2$$

object is revolving around

**Newton's 2nd Law (Angular Version):**  $\sum \tau = I\alpha$

**Static Equilibrium:**  $\sum F_x = \sum F_y = \sum \tau = 0$



## Rotational Kinetic Energy (Joules) and Angular Momentum (kg·m/s)

**Rotational Kinetic Energy:**  $K = \frac{1}{2}mv^2$  (translational KE) +  $\frac{1}{2}I\omega^2$  (rotational KE)

**Rolling without slipping:**  $\mathbf{v}_{\text{center-of-mass}} = \mathbf{v}_{\text{tan}}$ , at rim =  $r\omega$ .

**Angular Momentum:**  $\mathbf{L} = I\omega$ . Just as  $\mathbf{F}_{\text{avg}} = \Delta\mathbf{p}/\Delta t$ ,  $\tau = \Delta\mathbf{L}/\Delta t$ .

**Conservation Laws:** if  $\sum \mathbf{F}_{\text{ext}} = 0$ , then  $\Delta\mathbf{p} = 0$  and if  $\sum \tau_{\text{ext}} = 0$ ,  $\Delta\mathbf{L} = 0$ .

If  $\Delta\mathbf{L} = 0$ , then  $I_{1i}\omega_{1i} + I_{2i}\omega_{2i} = I_{1f}\omega_{1f} + I_{2f}\omega_{2f}$ .

**Harmonic Motion**      Spring Period:  $T = 2\pi\sqrt{\frac{m}{k_s}}$       Pendulum Oscillations:  $T = 2\pi\sqrt{\frac{\ell}{g}}$

Spring Oscillations and Circular Motion:

Amplitude:  $A = x_{\max}$

Position:  $x(t) = A \cos(\omega t)$

Velocity:  $v(t) = r\omega = A\omega \sin(\omega t)$

Acceleration:  $a(t) = r\omega^2 = A\omega^2 \cos(\omega t)$

Frequency:  $f = 1/T$

Angular Frequency:  $\omega = 2\pi f = 2\pi/T$

Mechanical Energy:  $E = \frac{1}{2}mv^2 + \frac{1}{2}kx^2 = \frac{1}{2}kA^2$

## **Fluids**

Density:  $\rho = \text{Mass/Volume (kg/m}^3\text{)}$ . Since  $m = \rho V$ ,  $F_{\text{grav}} = mg = \rho Vg$  for fluids.

Pressure:  $P = \text{Force/Area (N/m}^2\text{ or Pascals)}$

Pascal's Principle:  $P_{\text{bot}} = P_{\text{top}} + \rho gh$ , "gauge pressure" =  $P_{\text{bot}} - P_{\text{top}}$ .

Continuity Equation:  $Q$  (flow rate) = (area)\*(velocity) =  $Av$  ( $\text{m}^3/\text{s}$ ),  $A_1v_1 = A_2v_2$

Bernoulli's Equation:  $P_{\text{bot}} + \rho gy_{\text{bot}} + \frac{1}{2}\rho v_{\text{bot}}^2 = P_{\text{top}} + \rho gy_{\text{top}} + \frac{1}{2}\rho v_{\text{top}}^2$

or  $(P_{\text{bot}} - P_{\text{top}}) + \rho g(y_{\text{bot}} - y_{\text{top}}) + \frac{1}{2}\rho(v_{\text{bot}}^2 - v_{\text{top}}^2) = 0$

## **Thermal Physics**

Thermal Expansion (length):  $\Delta L = L_0\alpha\Delta T$ , where  $\alpha$  = linear expansion coefficient,  $\Delta T$  in  $^{\circ}\text{C}$  or  $\text{K}$ .

Thermal Expansion (area):  $\Delta A = A_0(2\alpha)\Delta T$  or  $A_0\beta\Delta T$ , where  $\beta$  = area expansion coefficient

Thermal Expansion (volume):  $\Delta V = V_0(3\alpha)\Delta T$  or  $V_0\gamma\Delta T$ , where  $\gamma$  = volume expansion coefficient

## **Calorimetry and Phase Changes**

Heat:  $Q$  (Joules),  $\Delta Q = mc\Delta T$ , where  $c$  = specific heat ( $\text{J/kg}\cdot^{\circ}\text{C}$ ),  $\Delta T$  in  $^{\circ}\text{C}$  or  $\text{K}$ .

Phase changes:  $\Delta Q = +mL_f$  (melting, solid  $\rightarrow$  liquid),  $-mL_f$  (freezing, liquid  $\rightarrow$  solid)

$\Delta Q = +mL_v$  (boiling, liquid  $\rightarrow$  gas),  $-mL_v$  (condensing, gas  $\rightarrow$  liquid)

where  $L_f$  = latent heat of fusion,  $L_v$  = latent heat of vaporization

Thermal Equilibrium:  $\Delta Q_1 + \Delta Q_2 + \Delta Q_3 + \dots = 0$

## **Heat Transfer (Watts)**

Conduction: Power ( $P$ ) =  $\Delta Q/\Delta t = \text{Area}\cdot\Delta T/R\text{-value}$ , where  $R\text{-value} = \ell_1/k_1 + \ell_2/k_2 + \ell_3/k_3 + \dots$

and  $\ell$  = layer thickness,  $k$  = thermal conductivity ( $\text{Joule/s}\cdot\text{m}\cdot^{\circ}\text{C}$ ) of each layer

Radiation: Power ( $P$ ) =  $\Delta Q/\Delta t = \sigma\cdot(\text{Area})\cdot e\cdot(T^4 - T_0^4)$ , where  $\sigma$  = S-B constant ( $5.67 \times 10^{-8} \text{ W/m}^2\cdot\text{K}^4$ ),

$e$  = emissivity (0-1),  $T$  = object temperature,  $T_0$  = temperature of surroundings

## **Ideal Gases**

$PV = nRT$  or  $PV = Nk_bT$

$R$  = Ideal gas constant (see p1)

$m$  = total gas mass (kg)

$P$  = Pressure ( $\text{N/m}^2$  or Pa)

$k_b$  = Boltzmann's constant (see p1)

$M$  = molar mass (kg/mole)

$V$  = Volume ( $\text{m}^3$ )

$n$  = # of moles

$n = m/M$

$T$  = Temperature (K)

$N$  = # of molecules

$n = N/N_A$  (see p1 for  $N_A$ )

## **Thermodynamics**

Calculating Work:  $W_{\text{by gas}} = +P_{\text{avg}}\Delta V$ ,  $W_{\text{on gas}} = -P_{\text{avg}}\Delta V$

Internal Energy:  $\Delta U = Q - W_{\text{by gas}} = Q + W_{\text{on gas}}$ , where  $U$  = Internal Energy (Joules),

and  $Q$  = heat added to gas (system)

Cyclic Process:  $\Delta U_{\text{cycle}} = 0$

Kinetic Energy of a Particle:  $KE = \frac{1}{2}m_{\text{particle}}v_{\text{rms}}^2 = 1.5k_bT$

Internal Energy of a Gas:  $U = 1.5nRT = 1.5PV$

## Sound Waves

Sound Waves in Air:  $v_{wave} = \sqrt{\frac{\gamma k_b T}{m}}$ ,  $\gamma = 5/3$  for ideal monatomic gas,  $7/5$  for ideal diatomic gas

$k_b =$  Boltzmann's constant (see pl),  $m =$  molecular mass (kg)

Sound Intensity:  $\beta$  (decibels) =  $10 \log (I/I_0)$ , where  $I_0 =$  hearing threshold,  $1.0 \times 10^{-12}$  W/m<sup>2</sup>.

$\Delta\beta$  (decibels) =  $10 \log (I_{big}/I_{small})$

Intensity of a Point Source:  $I$  (Watts/m<sup>2</sup>) = Power/ $4\pi r^2$

Wave Equation:  $v = f\lambda$

## Electric Forces (Newtons) and Electric Fields (N/C or V/m)

Electric Field (point charge):  $|\mathbf{E}| = k_c q/r^2$ , direction: away from + charges, toward - charges

Electric Field (sheet of charge):  $|\mathbf{E}| = 2\pi k_c \sigma$ , where  $\sigma =$  surface charge density (Q/Area)

Parallel sheets/plates:  $|\mathbf{E}| = 4\pi k_c \sigma$  inside, 0 outside, assuming equal and opposite Q on plates.

Conductors:  $|\mathbf{E}| = 0$  inside, all charge resides on surface, no charge enclosed by surface.

## Electric Potential (Volts) and Electric Potential Energy (Joules)

Absolute Potential (point charges):  $V_{abs} = k_c q/r$

Relative Potential:  $\Delta U_E = q_1 \Delta V_2$  for charge  $q_1$  immersed in potential from source 2.

Uniform Electric Fields:  $\Delta V = \pm \mathbf{E} \cdot (\text{distance})$ ,  $\mathbf{E}$  points from higher V to lower V.

Sign Conventions: + charges tend to follow E lines from higher to lower potential (voltage)

+ charges tend to follow E lines from higher to lower potential energy

If - charges follow E lines, they go against electric force and move from

higher to lower potential (voltage), lower to higher potential energy

Work-Energy:  $W_E = -\Delta U_E = -q_1 \Delta V_2$  for charge  $q_1$  immersed in potential from source 2.

## DC Circuits

Current:  $I$  (Amperes) =  $\Delta Q/\Delta t$

Resistance:  $R$  (Ohms) =  $\rho L/A$ , where  $\rho =$  resistivity (Ohm·meters),  $L =$  wire length,  $A =$  wire area

Ohm's Law:  $\Delta V$  (Volts) =  $\pm IR$  (current travels from higher to lower voltage)

Power:  $P$  (Watts) =  $I^2 R$  (power dissipated by resistor)

=  $I\Delta V$  (power supplied by source)

## Resistor Circuits

Series Resistors:  $R_{tot} = R_1 + R_2$ ,  $I_{tot} = I_1 = I_2$ ,  $\Delta V_{tot} = \Delta V_1 + \Delta V_2$

Parallel Resistors:  $1/R_{tot} = 1/R_1 + 1/R_2$ ,  $I_{tot} = I_1 + I_2$ ,  $\Delta V_{tot} = \Delta V_1 = \Delta V_2$

## Kirchoff's Laws

Loop Rule: The sum of all voltage drops around a loop is zero.  $\sum \Delta V = 0$ .

Junction Rule: At any junction, the sum of incoming currents = sum of outgoing currents.

## Capacitors

Capacitance:  $C$  (Farads) =  $Q/\Delta V = \text{Area} \cdot \epsilon_0/d = \text{Area}/4\pi \cdot k_c \cdot d$

Dielectrics:  $\kappa$  (kappa) = Dielectric constant.  $C_{new} = \kappa C_{original}$

Energy Stored by a Capacitor:  $U_E = \frac{1}{2} C \Delta V^2 = \frac{1}{2} Q \Delta V = Q^2/2C$

## RC Circuits (initially uncharged)

Capacitive Time Constant:  $\tau_c = RC$

Charge:  $Q(t) = C\mathcal{E}(1 - e^{-t/\tau_c})$ ,  $Q_{max} = C\mathcal{E}$

Current:  $I(t) = \left(\frac{\mathcal{E}}{R}\right)e^{-t/\tau_c}$ ,  $I_{max} = \mathcal{E}/R$

Capacitor Voltage:  $\Delta V_C = \mathcal{E}(1 - e^{-t/\tau_c})$ ,  $\Delta V_{max} = \mathcal{E}$

Resistor Voltage:  $\Delta V_R = \mathcal{E}e^{-t/\tau_c}$ ,  $\Delta V_{max} = \mathcal{E}$

## RL Circuits (with $I_{\text{initial}} = 0$ at $t = 0$ )

Inductive Time Constant:  $\tau_L = L/R$

Current:  $I(t) = \frac{\mathcal{E}}{R}(1 - e^{-t/\tau_L})$ ,  $I_{\text{max}} = \mathcal{E}/R$

Inductor Voltage:  $\Delta V_L = \mathcal{E}e^{-t/\tau_L}$ ,  $\Delta V_{\text{max}} = \mathcal{E}$

## Magnetic Fields (Tesla) and Magnetic Forces (Newtons)

### Right-hand rules

RHR #1 (cross products):  $\mathbf{A} = \mathbf{B} \times \mathbf{C}$ ,  $\mathbf{A}$  = palm,  $\mathbf{B}$  = thumb,  $\mathbf{C}$  = fingers

RHR #2 (magnetic field of straight wire):  $\mathbf{I}$  = thumb,  $\mathbf{B}$  = curl of fingers of right hand

RHR #3 (magnetic field of wire loop):  $\mathbf{I}$  = curl of fingers of right hand,  $\mathbf{B}_{\text{loop}}$  = thumb

Magnetic Field of a Wire:  $|\mathbf{B}| = \mu_0 I / 2\pi r$ , Direction: RHR #2

Magnetic Field of a Loop:  $|\mathbf{B}| = \mu_0 I / 2R$  within the plane of the loop and inside loop,  
where  $R$  = radius of loop, Direction: RHR #3

Magnetic Field of a Solenoid:  $|\mathbf{B}| = \mu_0 NI / L$  within the cylindrical volume of solenoid,  
 $N$  = # of turns,  $L$  = length of solenoid, use RHR #3

### Magnetic Force

Force on a moving charge:  $\mathbf{F}_B = q\mathbf{v} \times \mathbf{B}$ ,  $|\mathbf{F}_B| = |q\mathbf{v}\mathbf{B}\sin(\theta)|$ ,  $\theta$  = angle between  $\mathbf{v}$  and  $\mathbf{B}$ . RHR #1

Circular motion: Circular path of charge in a magnetic field has radius  $r = mv/qB$

Force on a current-carrying wire:  $\mathbf{F}_B = \ell \mathbf{I} \times \mathbf{B}$ ,  $|\mathbf{F}_B| = |\ell \mathbf{I}\mathbf{B}\sin(\theta)|$ ,  $\ell$  = length of wire. RHR #1

### Magnetic Torque

Magnetic Moment:  $\boldsymbol{\mu}$  ( $\text{T}\cdot\text{m}^2$ ) =  $N\mathbf{I}\mathbf{A}$ , where  $N$  = # of turns,  $\mathbf{A}$  = area of loop,  
direction is consistent with  $\mathbf{B}_{\text{loop}}$  from RHR #3.

Area vector:  $\mathbf{A}$  is normal to plane of loop, typically same direction as magnetic moment

Magnetic Torque:  $|\boldsymbol{\tau}_B| = |N\mathbf{B}_{\text{ext}}\mathbf{I}\mathbf{A}\sin(\theta)|$ ,  $\theta$  = angle between area vector and external magnetic field  
 $= \boldsymbol{\mu} \times \mathbf{B}_{\text{ext}} = |\boldsymbol{\mu}\mathbf{B}_{\text{ext}}\sin(\theta)|$

Direction: tends to align area vector (or  $\boldsymbol{\mu}$ ) with  $\mathbf{B}_{\text{ext}}$  direction.

## Electromagnetic Induction

Magnetic Flux:  $\Phi_B = |\mathbf{B}| \cdot |\mathbf{A}| \cdot \cos(\theta)$ , where  $\theta$  = angle between  $\mathbf{B}$  and Area vector ( $\mathbf{A}$ ).

Induced EMF:  $\mathcal{E}_{\text{ind}} = N(\Delta\Phi/\Delta t)$ , opposes  $\Delta\Phi$ .

Motional EMF:  $\mathcal{E}_{\text{ind}} = BLv$ , opposes  $\Delta\Phi$ .

Self-induction:  $\mathcal{E}_{\text{ind}} = L(\Delta I/\Delta t)$ , where  $L$  = self-inductance (Henrys),  $L_{\text{loop}} = N\Phi/I$

Energy Stored by an Inductor:  $E = \frac{1}{2}LI^2$

Finding direction of induced current:

1) Find initial direction of  $\Phi_B$ .

2) Find direction of  $\Delta\Phi_B$ .

3)  $B_{\text{ind}}$  opposed  $\Delta\Phi_B$ .

4)  $I_{\text{ind}}$  is consistent with  $B_{\text{ind}}$  using RHR #3

Average voltage drop across inductor:  $\Delta V_L = \pm L(\Delta I/\Delta t)$  (for instantaneous  $\Delta V_L$  - see RL circuits)

## Light and Optics

Energy Density of Light:  $u_{\text{tot}} = u_{\text{electric}} + u_{\text{magnetic}} = \frac{1}{2}\epsilon_0 E_{\text{rms}}^2 + \frac{1}{2}(1/\mu_0)B_{\text{rms}}^2$  OR  $u_{\text{tot}} = \epsilon_0 E_{\text{rms}}^2 = (1/\mu_0)B_{\text{rms}}^2$

Intensity of Light:  $S = \text{Power/Area} = c \cdot u_{\text{total}}$ , for light spread out over sphere,  $S = \text{Power}/4\pi r^2$

### Doppler Effect

General case (both source and observer moving):

Plus sign when source and observer come closer (blueshift)

Minus sign when source and observer move apart (redshift)

$$f_{\text{obs}} = f_{\text{src}} \left( 1 \pm \frac{v_{\text{rel}}}{v_{\text{wave}}} \right)$$

Alternate formula for Doppler effect:  $\frac{\Delta\lambda}{\lambda} = \frac{v_{\text{relative}}}{c}$

Wave Equation:  $v = f\lambda$

Index of refraction:  $n = c/v$ , where  $c$  = speed of light in vacuum,  $v$  = speed of light in medium

Wavelength of light:  $\lambda_n = \lambda_0/n$  (wavelength of light shortens when it enters some medium)

Snell's Law:  $n_1 \sin(\theta_1) = n_2 \sin(\theta_2)$ , light turns toward normal when entering higher index

Critical Angle:  $\theta_{\text{crit}} = \sin^{-1}(n_1/n_2)$ , max angle of incidence for light to pass from  $n_2 \rightarrow n_1$ .

### Polarization

Brewster's Angle:  $\theta_B = \tan^{-1}(n)$ . If  $\theta_{\text{incidence}} = \theta_B$ , ray is polarized parallel to surface

Unpolarized light through polarizer:  $I_{\text{final}} = \frac{1}{2}I_{\text{initial}}$

Polarized light through polarizer:  $I_{\text{final}} = I_{\text{initial}} \cos^2(\theta)$ ,

where  $\theta$  = angle between polarized light and axis of polarizer

### Lenses and Mirrors

$p$  = object distance

$q$  = image distance

$f$  = focal length

$R$  = radius of curvature =  $2f$

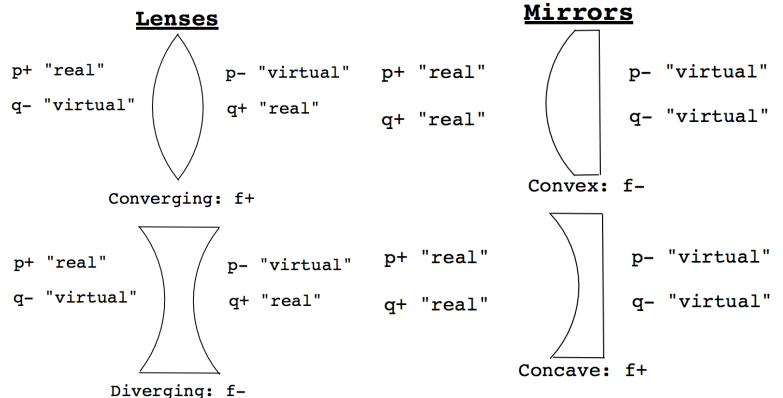
$M$  = magnification =  $-q/p$

If  $M+$ , image is upright

If  $M-$ , image is inverted

Image size:  $h_{\text{image}} = |M|h_{\text{object}}$

Optics Equation:  $\frac{1}{p} + \frac{1}{q} = \frac{1}{f}$



### Interference and Diffraction (light waves)

$d$  = slit separation,  $L$  = distance to screen,  $y$  = distance from center of pattern on wall,

$\delta$  = path difference between two sources of light,  $\theta$  = angular distance from center of pattern.

Two-slit interference ( $m$  = order number)

Constructive Interference (bright fringes) where  $\delta = d\sin\theta = dy/L = 0, \lambda, 2\lambda, 3\lambda, \dots (m\lambda)$

Destructive Interference (dark fringes) where  $\delta = dy/L = 0.5\lambda, 1.5\lambda, 2.5\lambda, \dots (m + \frac{1}{2})\lambda$

Single-slit interference

$a$  = slit width, dark fringes where  $a \sin\theta = ay/L = \lambda, 2\lambda, 3\lambda, \dots$

Resolution:  $\theta_{\text{min}} = \text{separation/distance} = \lambda/D$  (slit) or  $1.22\lambda/D$  (circular aperture)

Diffraction grating

$d$  = groove separation, bright light reflected where  $d\sin\theta = \lambda, 2\lambda, 3\lambda, \dots$

Thin Films

Phase shift due to reflection:  $\delta = \frac{1}{2}$  wave if reflecting off higher index, otherwise 0

Phase shift due to extra distance in film:  $\delta = 2tn/\lambda_0$  waves where  $t$  = film thickness

Constructive Interference (CI):  $\delta_2 - \delta_1 = 0, 1, 2, \dots$  waves, DI:  $\delta_2 - \delta_1 = 0.5, 1.5, 2.5$  waves

## Modern Physics

### Photoelectric Effect

Photon Energy:  $E = hf = hc/\lambda$ , where  $h$  = Planck's constant (see p1)

Work Function:  $\Phi$  = minimum KE needed for an electron to escape from a metal surface

Photoelectric Effect:  $(KE)_{\max} = hf - \Phi$  for max KE of electrons emerging from a surface

If  $hf < \Phi$ , then no electrons escape

$hf = \Phi$  at cutoff frequency:  $f_{\text{cutoff}} = \Phi/h$

Momentum of a photon:  $p = \text{Energy}/c = h/\lambda$

### Hydrogen spectrum

Energy levels in Hydrogen:  $E_n = -13.6/n^2$  eV, where 1 eV =  $1.60 \times 10^{-19}$  J

Electron absorption/emission:  $\frac{1}{\lambda} = R_H \left| \frac{1}{n_1^2} - \frac{1}{n_2^2} \right|$ , where  $R_H$  = Rydberg constant ( $1.097 \times 10^7 \text{ m}^{-1}$ )

Blackbody Radiation - Wien's Law:  $\lambda_{\max} T = 0.029 \text{ m}\cdot\text{K}$

### Radioactivity

Half-life:  $T_{1/2}$  = Time for half of the remaining radioactive atoms in a sample to decay

Decay constant:  $\lambda = 0.693/T_{1/2} \text{ s}^{-1}$

Radioactive decay:  $N(t) = N_0 e^{-\lambda t}$

Radioactivity:  $a(t) = \lambda N(t)$ ,  $a(t) = a_0 e^{-\lambda t}$ , units: Becquerels or Bq (decays/sec)

### Biological Effects of Radiation

Radiation Absorbed Dose (Grays): Dose = (Absorbed Energy)/(Mass of absorbing material)

1 rad = 0.01 J/kg = 0.01 Grays

Biologically Equivalent Dose (rems) = Absorbed Dose \* (Relative Biological Effectiveness)

### Nuclear Physics

Binding Energy:  $BE = \Delta mc^2$ , where  $\Delta m = M_{\text{nucleus}} - N_{\text{protons}} m_{\text{proton}} - N_{\text{neutrons}} m_{\text{neutron}}$

Mass-Energy calculations:  $E(\text{MeV}) = \text{Mass (u)} * 931.5 \text{ MeV/u}\cdot\text{c}^2$

### Masses of Selected Isotopes:

Proton: 1.007276 u

Neutron: 1.008665 u

Electron: 0.0005486 u

Hydrogen ( $^1\text{H}$ ): 1.007825 u      Deuterium ( $^2\text{H}$ ): 2.014102 u      Tritium ( $^3\text{H}$ ): 3.016050 u

Helium  $^3\text{He}$ : 3.016030 u       $^4\text{He}$ : 4.002602 u

Boron  $^{11}\text{B}$ : 11.009305 u

Carbon  $^{12}\text{C}$ : 12.000000 u       $^{13}\text{C}$ : 13.003355 u       $^{14}\text{C}$ : 14.003241 u

Manganese  $^{55}\text{Mn}$ : 54.938047 u

Iron  $^{56}\text{Fe}$ : 55.934939 u

Cobalt  $^{59}\text{Co}$ : 58.933198 u       $^{60}\text{Co}$ : 59.933819 u

Strontium  $^{90}\text{Sr}$ : 89.907738 u

Krypton  $^{92}\text{Kr}$ : 91.926270 u

Barium  $^{141}\text{Ba}$ : 140.914363 u

Radium  $^{226}\text{Ra}$ : 226.025402 u

Uranium  $^{235}\text{U}$ : 235.043924 u       $^{238}\text{U}$ : 238.050784 u

Plutonium  $^{242}\text{Pu}$ : 242.058737 u