

### Quiz 20.1A

A circuit contains a 120-Volt battery, a 5.6-Ohm resistor and a 22  $\mu\text{F}$  capacitor. At  $t=0$ , the capacitor is uncharged, and a switch is closed allowing current to begin to flow in the circuit to charge the capacitor.

- a) After 2.5 time constants have elapsed, what is the voltage drop across the capacitor?
- b) At this time, what is the voltage drop across the resistor?
- c) At what time is the voltage drop across the resistor equal to the voltage drop across the capacitor?

$$a) \quad Q(t) = Q_{\max}(1 - e^{-t/\tau})$$
$$Q(t = 2.5\tau) = CE(1 - e^{-2.5})$$

$$\Delta V = \frac{Q}{C} = E(1 - e^{-2.5})$$
$$= 120(0.918) = \boxed{110 \text{ Volts}}$$

$$b) \quad \text{Loop rules } \Delta V_C + \Delta V_R = E$$
$$110 + \Delta V_R = E \quad \boxed{\Delta V_R = 10 \text{ Volts}}$$

$$c) \quad \text{When } \Delta V_C = \Delta V_R, \text{ both are } 60 \text{ Volts}$$
$$60 + 60 = 120.$$

$$60 = 120(1 - e^{-t/\tau})$$
$$\frac{1}{2} = 1 - e^{-t/\tau}$$
$$\ln\left(\frac{1}{2}\right) = -\frac{t}{\tau}$$
$$t = 0.693\tau$$
$$= 0.693RC$$
$$= \boxed{8.5 \times 10^{-5} \text{ s}}$$